EUCLIDIAN GEOMETRY

Theorem 1

A line drawn from the centre of a circle, perpendicular to a chord, bisects the chord. "line from centre \perp to chord"

Theorem 1 (converse)

A line drawn from the centre of a circle, to the midpoint of a chord, will be perpendicular to the chord. *"line through centre and midpoint"*



Theorem 2

The perpendicular bisector of a chord passes through the centre of the circle. "perp. bisector of chord"

Theorem 3

The angle subtended by an arc at the centre of a circle is double the size of the angle subtended by the same arc at any point on the circumference of the circle. " \angle at centre = 2x \angle at circumf."



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Theorem 3 (collories)

 \rightarrow The diameter subtends a right angle at the circumference of the circle.

 \rightarrow If the angle at the circumference of a circle is a right angle, it is subtended by the diameter.

"∠ in semi-circle"

Theorem 4

The angles on a circle, subtended by a chord of the circle on the same side of the chord are equal. " \angle 's in the same segment"

Theorem 4 (collories)

Equal chords subtend equal angles at the circumference of a circle r'= chords subtends = 2's''

Theorem 4 (converse)

If two angles subtended by the same line are equal, then *ABCD* is a cyclic quadrilateral " \angle 's in the same segment"

Theorem 5

The opposite angles of a cyclic quadrilateral are supplementary . "opp. \angle 's of cyclic quad"

Theorem 5 (corollaries)

The exterior angle of a cyclic quadrilateral is equal to the opposite interior angle.

"Ext ∠ of cyclic quad."

Theorem 5 (converse)

A quadrilateral is a cyclic quadrilateral if the opposite angles are supplementary. "opp. \angle 's of quad suppl."

Theorem 6

Two tangents drawn to a circle from the same point outside the circle are equal in length. "tans. from same point"

Theorem 7

The angle between the tangent and the chord is equal to the angle subtended in the alternate segment.

"Tan-chord theorem"



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