

NATIONAL SENIOR CERTIFICATE EXAMINATION NOVEMBER 2016

EXAMINATION NUMBER

Time: 3 hours

150 marks

MATHEMATICS: PAPER II

PLEASE READ THE FOLLOWING INSTRUCTIONS CAREFULLY

- 1. This question paper consists of 27 pages and an Information Sheet of 2 pages (i–ii). Please check that your paper is complete.
- 2. Read the questions carefully.
- 3. Answer ALL the questions on the question paper and hand this in at the end of the examination. Remember to write your examination number on the space provided.
- 4. Number your answers exactly as the questions are numbered.
- 5. Diagrams are not necessarily drawn to scale.
- 6. You may use an approved non-programmable and non-graphical calculator, unless otherwise stated.
- 7. Ensure that your calculator is in **DEGREE** mode.
- 8. Round off your answers to one decimal digit where necessary, unless otherwise stated.
- 9. All the necessary working details must be clearly shown.
- 10. It is in your own interest to write legibly and to present your work neatly.

FOR OFFICE USE ONLY: MARKER TO ENTER MARKS

Q1	Q2	Q3	Q4	Q5	Q6	Q7	Q8	Q9	Q10	Q11	Q12	TOTAL
	24	11	16	0	Q	12	10	16	11	0	17	/150

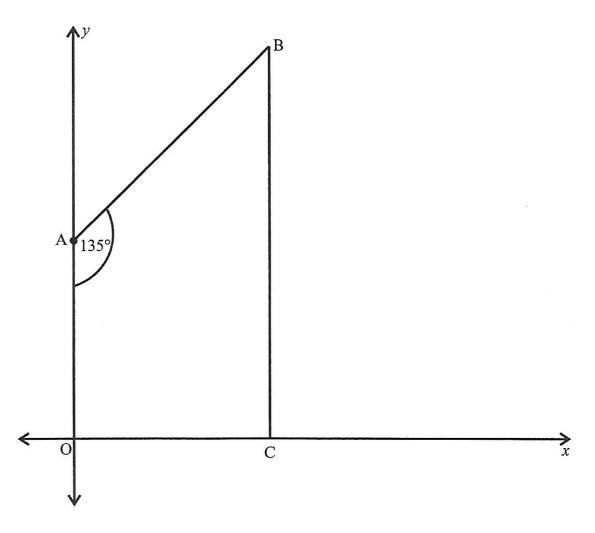
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SECTION A

QUESTION 1

In the diagram below, straight line AB makes an angle of 135° with the y-axis. AB cuts the y-axis at A.

B is joined to C, a point on the x-axis, so that BC is parallel to the y-axis.



COA Otas data	union the agreetion of the line AD	
OA = 8 units deter	mine the equation of the line AB.	

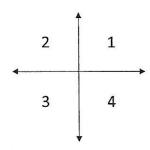
0	C = 6 units then determine	
(1)	the equation of BC.	
(0)		
(2)	the area of OCBA.	
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If
$$M = \frac{2\sin^2(180^\circ - \theta) + \sin 2\theta}{\cos 2\theta}$$
 and $P = \frac{2\sin \theta}{\cos \theta - \sin \theta}$

(a)	(1)	Prove that $M = P$.

(5)

- (b) If $\sin \beta = \frac{\sqrt{2}}{\sqrt{11}}$ and $\cos \beta < 0$ then
 - (1) In which quadrant is angle β ? (Circle the correct number) (1)

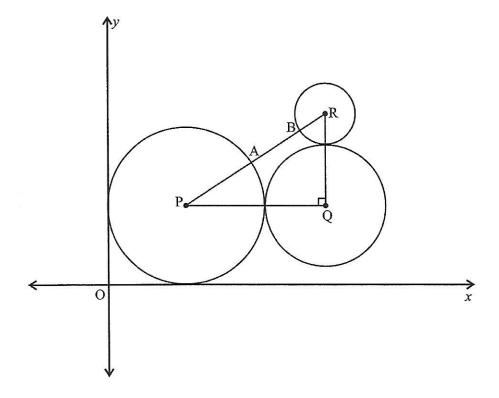


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(2)	Hence, determine the general solution to the equation: $\cos(\alpha - 30^{\circ}) - \cos(\alpha + 30^{\circ}) = 2\sin^{2}\alpha$
(2)	Hence, determine the general solution to the equation: $\cos(\alpha - 30^{\circ}) - \cos(\alpha + 30^{\circ}) = 2\sin^{2}\alpha$.
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In the diagram below:

- Circle P touches the x-axis and the y-axis.
- Circle P touches circle Q at one point.
- Circle Q touches circle R at one point.
- Circle P has a radius of 5 units.
- PQ is parallel to the x-axis and RQ is parallel to the y-axis.
- PR cuts the circles with centres P and R at A and B respectively.

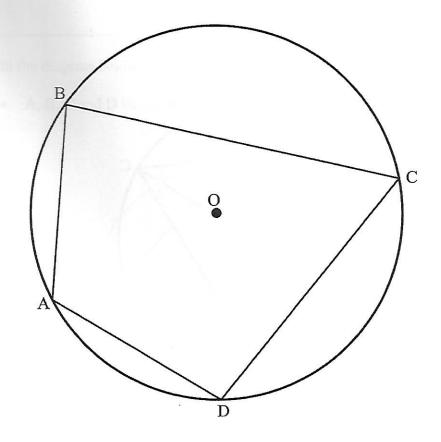


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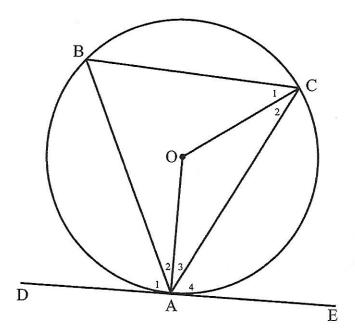
(a)

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	SAME II			
Determine the leng	gth of AB, correct to	two decimal d	igits.	
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(a) Use the diagram below to prove the theorem that states that the opposite angles of a cyclic quadrilateral are supplementary.



- (b) In the diagram below:
 - O is the centre of the circle.
 - A, B and C lie on the circumference of the circle.
 - Line DAE is a tangent to the circle at point A.
 - $\hat{A}_4 = 62^{\circ}$.
 - $\hat{A}_2 = 25^{\circ}$.



Calculate the size of a	ngle \hat{C}_1 .			
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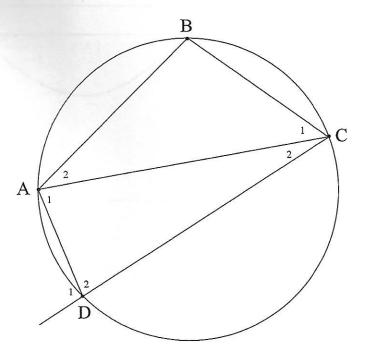
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(c) (1) What single statement can be deduced from both of the following statements?

$$M + N = D$$
$$M + Q = D$$

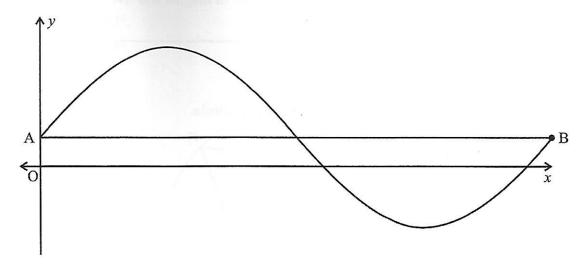
(1)

- (2) In the diagram below:
 - A, B, C and D lie on the circumference of the circle.



Prove that $\hat{B} = \hat{A}_1 + \hat{C}_2$	•		
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The graph of $f(x) = 3\sin x + 1$ with $x \in [0^\circ; 360^\circ]$ is drawn below. Line AB is parallel to the x-axis. A is a point on the y-axis.



(a) Write down the coordinates of point B.

		(2)
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(b) Calculate the value(s) for x where f(x) = -1 if $x \in [0^\circ; 360^\circ]$.

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(c) If g(x) = k and k is a constant term, then for what value(s) of k will f(x) = g(x) have no real solutions if $x \in [0^\circ; 180^\circ]$?

(4)

The manager of a hardware store records the number of staff that are in the store on a given day as well as the sales generated that day.

Staff	20	5	17	7	4	8	15	1	10	12	23	14
Sales in rand	35 200	9 200	32 000	15 600	9 200	17 200	31 200	3 000	19 600	26 800	39 200	20 800

			 A
Find the equatio	on for the line of best fi	it in the form $y =$	
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Total for Section A: 75 marks

SECTION B

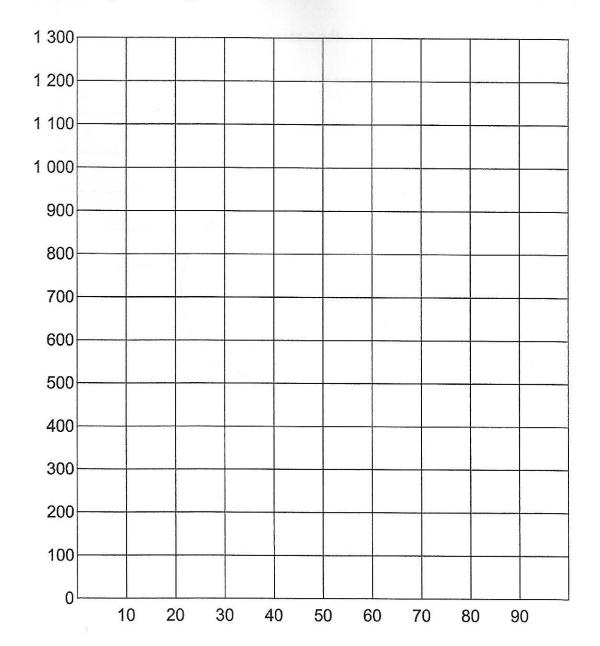
QUESTION 7

You develop a product and do some market research. The table below is a summary of the ages of people who say they will buy the product.

Age	Mid-point	Frequency	Cumulative Frequency
$5 < x \le 15$	10	200	200
$15 < x \le 25$	20	A	450
$25 < x \le 35$	30	20	470
$35 < x \le 45$	40	32	В
$45 < x \le 55$	50	23	525
$55 < x \le 65$	60	300	825
$65 < x \le 75$	70	475	1300

(1)	Calculate the estimated mean age of the people who say they will buy the product.

(c) Sketch the Ogive on the grid below.



(d) (1) Is the data normally distributed? Explain.

(2) You are developing a marketing strategy. Is the mean age a good indicator of how to advertise your product? Explain your answer.

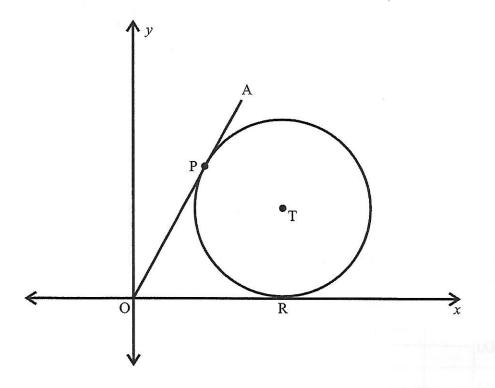
(2)

(3)

(2)

In the diagram below, circle centre T touches the x-axis at R.

- AO is a tangent to the circle at P.
- OT = 5 and TP = 3.



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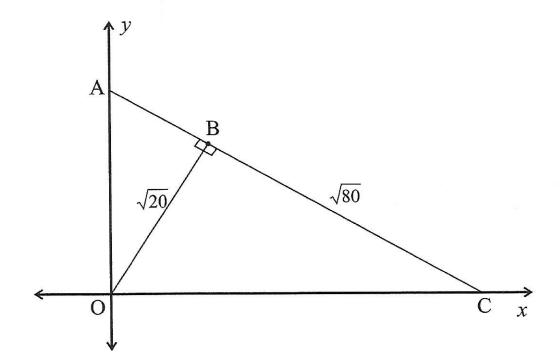
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In the diagram below, C and A are points on the x-axis and y-axis respectively.

- OB ⊥ AC.
- OB has a length of $\sqrt{20}$ units.
- BC has a length of $\sqrt{80}$ units.



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Calculate the coord	inates of point B.		
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(d)

(5) [**16**]

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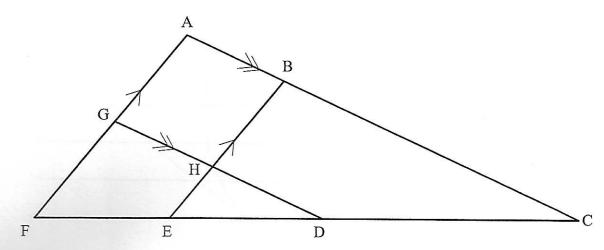
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The diagram below is the top view design of a new railway system. There are eight stations being built and these are labelled with letters from A-H.

You have been asked to do some calculations for the railway company.

As the engineer you know that:

- AF//BE and AC//GD.
- $\frac{AB}{BC} = \frac{4}{7}$ and $\frac{AG}{AF} = \frac{9}{17}$.



(a) Calculate $\frac{FE}{FC}$.

	- 180km			

(b) Calculate $\frac{CD}{DF}$.

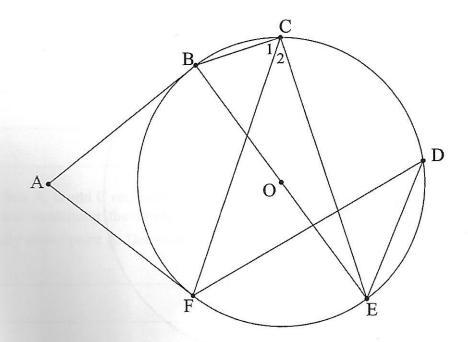
(3)

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In the diagram below:

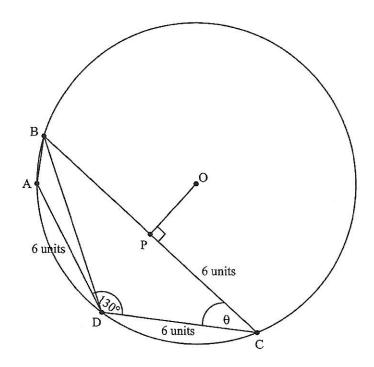
- B, C, D, E and F lie on the circle centre O.
- Lines AB and AF are tangents to the circle at B and F respectively.
- Line BE passes through O.



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If $\hat{D} = 38^\circ$ determine the size of $\hat{R}\hat{A}\hat{F}$	
If $\hat{D} = 38^{\circ}$, determine the size of BÂF.	
If $\hat{D} = 38^{\circ}$, determine the size of BÂF.	

In the diagram below:

- A, B, C and D lie on the circle centre O.
- P is a point on BC so that OP \perp BC.
- AD = DC = CP = 6 units.
- $\hat{ADC} = 130^{\circ} \text{ and } \hat{BCD} = \theta.$



	Qua.	
Show that $\hat{DBC} = 25^{\circ}$.		

Given that A. D. and	d C remain fixed points on the circle and that point R is lifted off
the plane containing	d C remain fixed points on the circle and that point B is lifted offing the circle and positioned at a point, T, which is 9 units int A. Determine TĈA.
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the plane containing	ng the circle and positioned at a point, T, which is 9 units
the plane containing	ng the circle and positioned at a point, T, which is 9 units

Total for Section B: 75 marks

Total: 150 marks