



MORNING SESSION

This question paper consists of 8 pages and 1 information sheet.

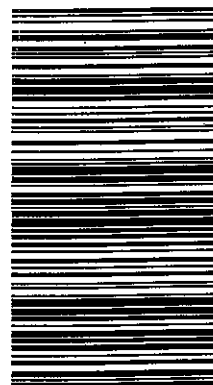
TIME: 3 hours

MARKS: 150

MATH.1
 MATHEMATICS P1
 NOVEMBER 2017

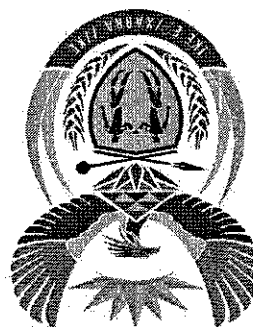
GRADE 12

NATIONAL SENIOR CERTIFICATE



Department:
 Basic Education
 REPUBLIC OF SOUTH AFRICA

basic education



QUESTION 1

1.1 Solve for x:

1.1.1 $x^2 + 9x + 14 = 0$

(3)

1.1.2 $4x^2 + 9x - 3 = 0$ (correct to TWO decimal places)

(4)

1.1.3 $\sqrt{x^2 - 5} = 2\sqrt{x}$

(4)

1.2 Solve for x and y if:

$3x - y = 4$ and $x^2 + 2xy - y^2 = -2$

(6)

1.3 Given: $f(x) = x^2 + 8x + 16$

1.3.1 Solve for x if $f(x) > 0$.

(3)

1.3.2 For which values of p will $f(x) = p$ have TWO unequal negative roots?

(4)

[24]

QUESTION 2

2.1

Given the following quadratic number pattern: 5 ; -4 ; -19 ; -40 ; ...

2.1.1 Determine the constant second difference of the sequence.

(2)

2.1.2 Determine the n^{th} term (T_n) of the pattern.

(4)

2.1.3 Which term of the pattern will be equal to -25 939?

(3)

2.2

The first three terms of an arithmetic sequence are $2k - 7$; $k + 8$ and $2k - 1$.

2.2.1 Calculate the value of the 15^{th} term of the sequence.

(5)

2.2.2 Calculate the sum of the first 30 even terms of the sequence.

(4)

[18]

QUESTION 3

A convergent geometric series consisting of only positive terms has first term a , constant ratio r and n^{th} term, T_n , such that $\sum_{n=3}^{\infty} T_n = \frac{1}{4}$.

3.1 If $T_1 + T_2 = 2$, write down an expression for a in terms of r .

(2)

3.2 Calculate the values of a and r .

(6)

[8]



QUESTION 4

Given: $f(x) = -ax^2 + bx + 6$

- 4.1 The gradient of the tangent to the graph of f at the point $\left(-1; \frac{7}{2}\right)$ is 3. Show that $a = \frac{1}{2}$ and $b = 2$. (5)
- 4.2 Calculate the x-intercepts of f . (3)
- 4.3 Calculate the coordinates of the turning point of f . (3)
- 4.4 Sketch the graph of f . Clearly indicate ALL intercepts with the axes and the turning point. (4)
- 4.5 Use the graph to determine the values of x for which $f(x) > 6$. (3)
- 4.6 Sketch the graph of $g(x) = -x - 1$ on the same set of axes as f . Clearly indicate ALL intercepts with the axes. (2)
- 4.7 Write down the values of x for which $f(x) \cdot g(x) \leq 0$. (3)

[23]

Please turn over.



WESTERN CAPE



QUESTIONS

The diagram below shows the graphs of $g(x) = \frac{x+d}{2} + q$ and $f(x) = \log_3 x$.

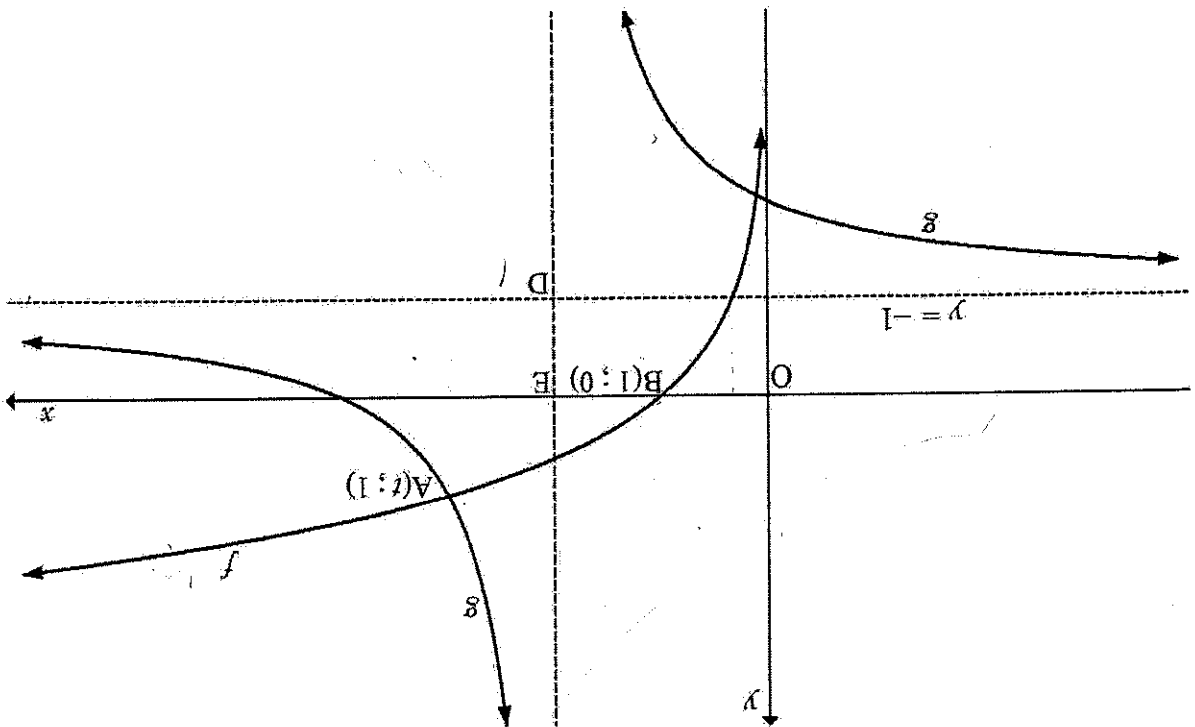
- $y = -1$ is the horizontal asymptote of g .

- $B(1; 0)$ is the x -intercept of f .

- $A(t; 1)$ is a point of intersection between f and g .

- The vertical asymptote of g intersects the x -axis at E and the horizontal asymptote at D .

- $OB = BE$.



5.1 Write down the range of g . (2)

5.2 Determine the equation of g . (2)

5.3 Calculate the value of t . (3)

5.4 Write down the equation of f^{-1} , the inverse of f , in the form $y = \dots$ (2)

5.5 For which values of x will $f^{-1}(x) < 3$? (2)

5.6 Determine the point of intersection of the graphs of f and the axis of symmetry of g that has a negative gradient. (3)

[14]

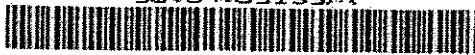


QUESTION 6

- 6.1 Mbali invested R10 000 for 3 years at an interest rate of r % p.a., compounded monthly. At the end of this period, she received R12 146,72. Calculate r , correct to ONE decimal place. (5)
- 6.2 Piet takes a loan from a bank to buy a car for R235 000. He agrees to repay the loan over a period of 54 months. The first instalment will be paid one month after the loan is granted. The bank charges interest at 11% p.a., compounded monthly. (4)
- 6.2.1 Calculate Piet's monthly instalment. (4)
- 6.2.2 Calculate the total amount of interest that Piet will pay during the first year of the repayment of the loan. (6)

QUESTION 7

- 7.1 Given: $f(x) = 2x^2 - x$
- 7.2 Determine $f'(x)$ from first principles. (6)
- 7.2.1 $D_x[(x+1)(3x-7)]$ (2)
- 7.2.2 $\frac{dy}{dx}$ if $y = \sqrt{x^3} - \frac{5}{x} + \frac{1}{2}\pi$ (4)
- [12]





QUESTION 8

Given: $f(x) = x(x-3)^2$ with $f'(1) = 0$ and $f(1) = 4$

8.1 Show that f has a point of inflection at $x = 2$. (5)

8.2 Sketch the graph of f , clearly indicating the intercepts with the axes and the turning points. (4)

8.3 For which values of x will $y = -f(x)$ be concave down? (2)

8.4 Use your graph to answer the following questions:

8.4.1 Determine the coordinates of the local maximum of h if $h(x) = f(x-2) + 3$. (2)

8.4.2 Claire claims that $f'(2) = 1$. (2)

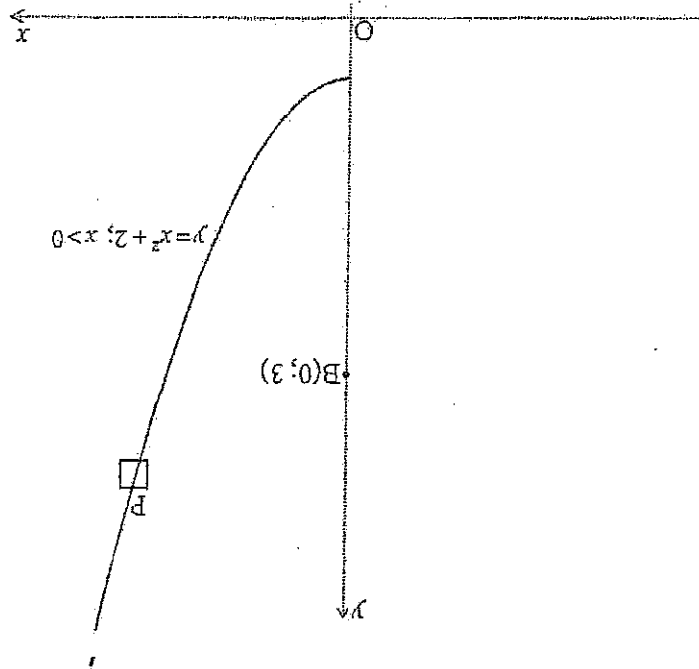
Do you agree with Claire? Justify your answer.

[15]

QUESTION 9

An aerial view of a stretch of road is shown in the diagram below. The road can be described by the function $y = x^2 + 2$, $x \geq 0$ if the coordinate axes (dotted lines) are chosen as shown in the diagram.

Benny sits at a vantage point $B(0; 3)$ and observes a car, P , travelling along the road.



Calculate the distance between Benny and the car, when the car is closest to Benny.

[7]



QUESTION 10

A survey was conducted among 100 Grade 12 learners about their use of Instagram (I), Twitter (T) and WhatsApp (W) on their cell phones. The survey revealed the following:

- 8 use all three.
- 12 use Instagram and Twitter.
- 5 use Twitter and WhatsApp, but not Instagram.
- x use Instagram and WhatsApp, but not Twitter.
- 61 use Instagram.
- 19 use Twitter.
- 73 use WhatsApp.
- 14 use none of these applications.

10.1 Draw a Venn diagram to illustrate the information above. (4)

10.2 Calculate the value of x. (2)

10.3 Calculate the probability that a learner, chosen randomly, uses only ONE of these applications. (2)

[8]

QUESTION 11

A company uses a coding system to identify its clients. Each code is made up of two letters and a sequence of digits, for example AD108 or RR 45789.

The letters are chosen from A, D, R; S and U. Letters may be repeated in the code.

The digits 0 to 9 are used, but NO digit may be repeated in the code.

11.1 How many different clients can be identified with a coding system that is made up of TWO letters and TWO digits? (3)

11.2 Determine the least number of digits that is required for a company to uniquely identify 700 000 clients using their coding system. (3)

[6]

TOTAL: 150

INFORMATION SHEET: MATHEMATICS

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$A = P(1 + i)^n \quad A = P(1 - i)^n$$

$$T_n = a + (n-1)d \quad S_n = \frac{n}{2}[2a + (n-1)d]$$

$$T_n = ar^{n-1} \quad S_n = \frac{a(r^n - 1)}{r - 1}; r \neq 1$$

$$F = \frac{x[(1+i)^n - 1]}{i} \quad P = \frac{x[1 - (1+i)^{-n}]}{i}$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$y = mx + c \quad y - y_1 = m(x - x_1)$$

$$(x-a)^2 + (y-b)^2 = r^2$$

$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\text{Area } \Delta ABC = \frac{1}{2} ab \sin C$$

$$\sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta$$

$$\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta$$

$$\sin(\alpha - \beta) = \sin \alpha \cos \beta - \cos \alpha \sin \beta$$

$$\cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$$

$$\left. \begin{aligned} \cos 2\alpha &= \cos^2 \alpha - \sin^2 \alpha \\ &= 1 - 2\sin^2 \alpha \\ &= 2\cos^2 \alpha - 1 \end{aligned} \right\}$$

$$\sin 2\alpha = 2 \sin \alpha \cos \alpha$$

$$\sigma^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n}$$

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

$$b = \frac{\sum (x-x)^2}{\sum (x-x)(y-y)}$$

$$\bar{x} = \frac{\sum x}{n}$$

$$\frac{P(A)}{P(S)} = \frac{n(A)}{n(S)}$$

$$y = a + bx$$

