



# basic education

Department:  
Basic Education  
**REPUBLIC OF SOUTH AFRICA**

NATIONAL  
SENIOR CERTIFICATE/  
*NASIONALE*  
*SENIOR SERTIFIKAAT*

**GRADE/GRAAD 11**

**MATHEMATICS P1/WISKUNDE V1**

**NOVEMBER 2017**

**MARKING GUIDELINES/NASIENRIGLYNE**

**MARKS/PUNTE: 150**

These marking guidelines consist of 19 pages.  
*Hierdie nasienriglyne bestaan uit 19 bladsye.*

*Govender*  
12/11/2017

*W. White*  
12/11/2017

**NOTE:**

- If a candidate answered a question TWICE, mark only the FIRST attempt.
- If a candidate crossed out an answer and did not redo it, mark the crossed-out answer.
- Consistent accuracy applies to ALL aspects of the marking guidelines.
- Assuming values/answers in order to solve a problem is unacceptable.

**LET WEL:**

- As 'n kandidaat 'n vraag TWEE keer beantwoord het, sien slegs die EERSTE poging na.
- As 'n kandidaat 'n antwoord deurgehaal en nie oorgedoen het nie, sien die deurgehaalde antwoord na.
- Volgehoue akkuraatheid is op ALLE aspekte van die nasienriglyne van toepassing.
- Dit is onaanvaarbaar om waardes/antwoorde te veronderstel om 'n probleem op te los.

**QUESTION/VRAAG 1**

1.1.1	$(2x - 3)(x + 7) = 0$ $x = \frac{3}{2}$ or $x = -7$	$\checkmark x = \frac{3}{2}$ $\checkmark x = -7$	(2)
-------	--	---	-----

1.1.2	$7x^2 + 3x - 2 = 0$ $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $= \frac{-(3) \pm \sqrt{(3)^2 - 4(7)(-2)}}{2(7)}$ $= \frac{-3 \pm \sqrt{65}}{14}$ $x = -0,79 \text{ or } x = 0,36$	$\checkmark$ substitution/vervanging  <div style="border: 1px solid black; padding: 5px;"><b>NOTE/LET WEL:</b> Penalty 1 mark for incorrect rounding Penalisering 1 punt vir verkeerde afronding</div> $\checkmark$ answer/antwoord $\checkmark$ answer/antwoord	
-------	---	--	--

**OR/ OF**

	$x^2 + \frac{3}{7}x - \frac{2}{7} = 0$ $x^2 + \frac{3}{7}x - \frac{9}{196} = \frac{2}{7} + \frac{9}{196}$ $\left(x + \frac{3}{14}\right)^2 = \frac{65}{196}$ $x + \frac{3}{14} = \frac{\pm\sqrt{65}}{14}$ $x = \frac{-3 \pm \sqrt{65}}{14}$ $x = -0,79 \text{ or } x = 0,36$	$\checkmark \left(x + \frac{3}{14}\right)^2 = \frac{65}{196}$  $\checkmark$ answer/antwoord $\checkmark$ answer/antwoord	(3)
--	---	---	-----

1.1.3	$\sqrt{x-1} + 3 = x$ $\sqrt{x-1} = x - 3$ $(\sqrt{x-1})^2 = (x-3)^2$ $x-1 = x^2 - 6x + 9$ $x^2 - 7x + 10 = 0$ $(x-2)(x-5) = 0$ $x \neq 2 \quad \text{or/of} \quad x = 5$	<ul style="list-style-type: none"> <li>✓ isolate/isooleer ✓ sign/teken</li> <li>✓ squaring/kwadr both sides/beide kante</li> <li>✓ std form/stand vorm</li> <li>✓ factors/fakt</li> <li>✓ <math>x = 5</math></li> <li>✓ <math>x \neq 2</math></li> </ul> <p style="text-align: right;">(6)</p>
1.1.4	$x^2 > 3(x+6)$ $x^2 - 3x - 18 > 0$ $(x-6)(x+3) > 0$ <b>OR/OF</b> $x < -3$ or $x > 6$ $x \in (-\infty ; -3) \cup (6 ; \infty)$	<ul style="list-style-type: none"> <li>✓ std form/vorm</li> <li>✓ factors/fakt</li> <li>✓ <math>x &lt; -3</math> <b>OR/OF</b> <math>(-\infty ; -3)</math></li> <li>✓ <math>x &gt; 6</math> <b>OR/OF</b> <math>(6 ; \infty)</math></li> </ul> <p style="text-align: right;">(4)</p>
1.2	$2y + x = 1$ $x = 1 - 2y$ $x^2 + y^2 + 3xy + y = 0$ $(1-2y)^2 + y^2 + 3y(1-2y) + y = 0$ $1-4y+4y^2+y^2+3y-6y^2+y=0$ $1-y^2=0$ $(1-y)(1+y)=0$ $y=1 \quad \text{or} \quad y=-1$ $x=-1 \quad \text{or} \quad x=3$ <b>OR/OF</b>	<ul style="list-style-type: none"> <li>✓ <math>x = 1 - 2y</math></li> <li>✓ substitution/verv</li> <li>✓ std form/stand vorm</li> <li>✓ factors/fakt</li> <li>✓ <math>y</math>-values/wrdes</li> <li>✓ <math>x</math>-values/wrdes</li> </ul>

	$2y + x = 1$ $y = \frac{1-x}{2}$ $x^2 + y^2 + 3xy + y = 0$ $x^2 + \left(\frac{1-x}{2}\right)^2 + 3x\left(\frac{1-x}{2}\right) + \frac{1-x}{2} = 0$ $x^2 + \frac{1-2x+x^2}{4} + \frac{3x-3x^2}{2} + \frac{1-x}{2} = 0$ $4x^2 + 1 - 2x + x^2 + 6x - 6x^2 + 2 - 2x = 0$ $-x^2 + 2x + 3 = 0$ $x^2 - 2x - 3 = 0$ $(x-3)(x+1) = 0$ $x=3 \quad or \quad x=-1$ $y=-1 \quad or \quad y=1$	$\checkmark y = \frac{1-x}{2}$ $\checkmark$ substitution/verv
1.3	$3-12k^2=0$ $1-4k^2=0$ $k^2 = \frac{1}{4}$ $k = \pm \frac{1}{2}$ $3-12k^2=0$ $1-4k^2=0$ $(1-2k)(1+2k)=0$ $k=\frac{1}{2} \text{ OR/OF } k=-\frac{1}{2}$	$\checkmark 3-12k^2=0$ $\checkmark k^2 = \frac{1}{4}$ $\checkmark k = \pm \frac{1}{2}$ $\checkmark 3-12k^2=0$ $\checkmark (1-2k)(1+2k)=0$ $\checkmark k = \pm \frac{1}{2}$
		(6) (3) (3)

[24]

**QUESTION/VRAAG 2**

2.1	$\begin{aligned} & \frac{3^{m+4} - 6 \cdot 3^{m+1}}{7 \cdot 3^{m+2}} \\ &= \frac{3^{m+1}(3^3 - 6)}{7 \cdot 3^{m+1} \cdot 3} \\ &= \frac{3^3 - 6}{7 \cdot 3} \\ &= \frac{21}{21} \\ &= 1 \end{aligned}$ <p><b>OR/OF</b></p> $\begin{aligned} & \frac{3^{m+4} - 6 \cdot 3^{m+1}}{7 \cdot 3^{m+2}} \\ &= \frac{3^m(3^4 - 6 \cdot 3)}{3^m(7 \cdot 3^2)} \\ &= \frac{3^m \cdot 63}{3^m \cdot 63} \\ &= 1 \end{aligned}$	<ul style="list-style-type: none"> <li>✓ common factor/gemene fakt</li> <li>✓ <math>3^3 - 6</math></li> <li>✓ simplification/vereenv.</li> <li>✓ answer/antw.</li> </ul>
2.2.1	$\begin{aligned} x^{-\frac{3}{4}} &= 8 \\ x^{-\frac{3}{4}} &= 2^3 \\ x &= (2^3)^{-\frac{4}{3}} \\ x &= 2^{-4} \\ x &= \frac{1}{16} \end{aligned}$ <p><b>OR/OF</b></p> $\begin{aligned} x^{-\frac{3}{4}} &= 8 \\ \sqrt[4]{x^{-3}} &= 2^3 \\ x^{-3} &= 2^{12} & (2^{12} = 4096) \\ x^{-1} &= 2^4 & (2^4 = 16) \\ x &= 2^{-4} \\ x &= \frac{1}{16} \end{aligned}$	<ul style="list-style-type: none"> <li>✓ <math>2^3</math></li> <li>✓ rational exponent/rasionele eksp</li> <li>✓ answer in any form/antw. in enige vorm</li> </ul>

<p><b>2.2.2</b></p> $2^{2x} - 2^x = 2$ $2^{2x} - 2^x - 2 = 0$ $(2^x + 1)(2^x - 2) = 0$ $2^x \neq -1 \quad \text{or} \quad 2^x = 2$ $x = 1$	<p><b>NOTE / LET WEL:</b></p> <p>If answer only of <math>x = 1</math>: award 1/4 marks  <i>Slegs antwoord van <math>x = 1</math>: gee 1/4 punte</i></p> <p>If the learner writes <math>2x - x = 1</math>      Breakdown: 0/4 marks  <i>As die leerder <math>2x - x = 1</math> skryf</i>  <i>Ontleding: 0/4 punte</i></p>	<p>✓ std vorm/stand vorm      ✓ factors/fakt      ✓ <math>x = 1</math>      ✓ <math>2^x \neq -1</math></p>
<p><b>2.3</b></p> $(x+y)^2 = \left( \frac{3-\sqrt{a}}{\sqrt{2}} + \frac{4+\sqrt{a}}{\sqrt{2}} \right)^2$ $= \left( \frac{7}{\sqrt{2}} \right)^2$ $= \frac{49}{2}$ $= 24\frac{1}{2}$	<p>✓ substitution/verv.</p>	<p>✓ simplification/vereenv.</p>
<p><b>OR/OF</b></p> $(x+y)^2 = x^2 + 2xy + y^2$ $= \left( \frac{3-\sqrt{a}}{\sqrt{2}} \right)^2 + 2 \left( \frac{3-\sqrt{a}}{\sqrt{2}} \right) \left( \frac{4+\sqrt{a}}{\sqrt{2}} \right) + \left( \frac{4+\sqrt{a}}{\sqrt{2}} \right)^2$ $= \left( \frac{9-6\sqrt{a}+a}{2} \right) + 2 \left( \frac{12-\sqrt{a}-a}{2} \right) + \left( \frac{16+8\sqrt{a}+a}{2} \right)$ $= \left( \frac{25+2\sqrt{a}+2a}{2} \right) + (12-\sqrt{a}-a)$ $= \frac{25}{2} + \sqrt{a} + a + 12 - \sqrt{a} - a$ $= 24\frac{1}{2}$	<p>✓ substitution/verv.</p>	<p>✓ simplification/vereenv.</p>
<p><b>OR/OF</b></p> $\begin{aligned} & \sqrt[12]{10} \cdot \sqrt[6]{64 \cdot 10} \cdot \sqrt[4]{81 \cdot 10} \cdot \sqrt{4 \cdot 10} \\ &= \sqrt[12]{10} \cdot \sqrt[6]{2^6 \cdot 10} \cdot \sqrt[4]{3^4 \cdot 10} \cdot \sqrt{2^2 \cdot 10} \\ &= 10^{\frac{1}{12}} \cdot 2^{\frac{6}{6}} \cdot 10^{\frac{1}{6}} \cdot 3^{\frac{4}{4}} \cdot 10^{\frac{1}{4}} \cdot 2^{\frac{2}{2}} \cdot 10^{\frac{1}{2}} \\ &= 2 \times 3 \times 2 \times 10^{\frac{12}{12}} \\ &= 120 \end{aligned}$	<p>✓ split the surd/  <i>skei wortel</i>      ✓ prime base/ <i>priem basis</i>      ✓ rational exponents/  <i>rasionele eksp</i>      ✓ <math>10^{\frac{12}{12}}</math></p>	<p>(3)</p>

$  \begin{aligned}  &= \sqrt[12]{2.5} \cdot \sqrt[6]{2^7 \cdot 5} \cdot \sqrt[4]{3^4 \cdot 2.5} \cdot \sqrt{2^3 \cdot 5} \\  &= 2^{\frac{1}{12}} \cdot 5^{\frac{1}{12}} \cdot 2^{\frac{7}{6}} \cdot 5^{\frac{1}{6}} \cdot 3^{\frac{4}{4}} \cdot 2^{\frac{1}{4}} \cdot 5^{\frac{1}{4}} \cdot 2^{\frac{3}{2}} \cdot 5^{\frac{1}{2}} \\  &= 2^{\frac{36}{12}} \times 3^{\frac{4}{4}} \times 5^{\frac{12}{12}} \\  &= 2^3 \times 3^1 \times 5^1 \\  &= 120  \end{aligned}  $	<ul style="list-style-type: none"> <li>✓ prime base/ <i>priem basis</i></li> <li>✓ rational exponents/ <i>rasionele eksp</i></li> <li>✓ exponent law/ <i>eksp. wet</i></li> <li>✓ simplification/ <i>vereenv</i></li> </ul> <p style="text-align: right;">(4)</p>
	[18]



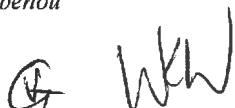
**QUESTION/VRAAG 3**

3.1.1	$T_n = 5n + 7$	✓ 5n ✓ +7 (2)
3.1.2	$\begin{aligned} T_{12} &= 5(12) + 7 \\ &= 67 \end{aligned}$	✓ subst/verv ✓ answer/antw (2)
3.1.3	$\begin{aligned} 5n + 7 &= 172 \\ 5n &= 165 \\ n &= 33 \end{aligned}$	✓ 5n + 7 = 172 ✓ answer/antw (2)
3.2	$\begin{aligned} x - 3 &= y - x \\ y &= 2x - 3 \\ x - 3 &= 30 - y \\ x - 3 &= 30 - 2x + 3 \\ 3x &= 36 \quad \text{OR/OF} \\ x &= 12 \\ y &= 21 \end{aligned}$ $\begin{aligned} 30 - y &= y - x \\ 30 + x &= 2y \\ 30 + x &= 2(2x - 3) \\ 36 &= 3x \\ 12 &= x \\ y &= 21 \end{aligned}$ $\begin{aligned} x &= 3 + 9 = 12 \\ y &= 12 + 9 = 21 \end{aligned}$	✓ $x - 3 = y - x$ ✓ $30 - y = y - x$ ✓ equating/verg. ✓ both /beide $x = 12$ and/en $y = 21$ (4) <b>OR/OF</b> ✓✓ $30 - 3 = 3d$ ✓ $d = 9$ ✓ both /beide $x = 12$ and/en $y = 21$ (4) [10]

**QUESTION/VRAAG 4**

4.1	<p><math>T_5 = 76</math></p> <div style="border: 1px solid black; padding: 5px; margin-top: 10px;"> <b>NOTE/LET WEL:</b>            Calc. differences 1/2 marks            bereken verskille: 1/2 punte         </div>	<span style="color: green;">✓✓</span> answer/antw. (2)
4.2	$\begin{aligned} 2a &= 6 \\ a &= 3 \\ 3a + b &= -51 \\ 3(3) + b &= -51 \\ b &= -60 \\ a + b + c &= 244 \\ 3 + -60 + c &= 244 \\ c &= 301 \\ T_n &= 3n^2 - 60n + 301 \end{aligned}$	<span style="color: green;">✓</span> $a = 3$ <span style="color: green;">✓</span> $b = -60$ <span style="color: green;">✓</span> $c = 301$ <span style="color: green;">✓</span> $T_n = 3n^2 - 60n + 301$ (4)
4.3	$\begin{aligned} 3n^2 - 60n + 301 &= 508 \\ 3n^2 - 60n - 207 &= 0 \\ n^2 - 20n - 69 &= 0 \\ (n + 3)(n - 23) &= 0 \\ n = 23 \text{ or } n &\neq -3 \end{aligned}$	<span style="color: green;">✓</span> equating/verg. <span style="color: green;">✓</span> std form/stand vorm <span style="color: green;">✓</span> factors/fakore <span style="color: green;">✓</span> select/kies $n = 23$ (4)
4.4	<p>using first diff./ gebruik eerste versk</p> $\begin{aligned} T_n &= 6n - 57 \\ 453 &= 6n - 57 \\ 510 &= 6n \\ n &= 85 \\ \text{between } T_{85} \text{ and } T_{86} \text{ in the quadratic pattern} \\ \text{tussen } T_{85} \text{ en } T_{86} \text{ in die kwadratiese patroon} \end{aligned}$ <p><b>OR/OF</b></p> <p>In the quadratic pattern / in die kwadratiese patroon</p> $\begin{aligned} T_{n+1} - T_n &= 453 \\ 3(n+1)^2 - 60(n+1) + 301 - (3n^2 - 60n + 301) &= 453 \\ 3n^2 + 6n + 3 - 60n - 60 - 3n^2 + 60n &= 453 \\ 6n &= 510 \\ n &= 85 \\ \text{between } T_{85} \text{ and } T_{86} \\ \text{tussen } T_{85} \text{ en } T_{86} \end{aligned}$	<span style="color: green;">✓</span> $6n - 57$ <span style="color: green;">✓</span> $453 = 6n - 57$  <span style="color: green;">✓</span> between $T_{85}$ and $T_{86}$ tussen $T_{85}$ en $T_{86}$ (3)

4.5	$  \begin{aligned}  T_n &= 3n^2 - 60n + 300 + 1 \\  &= 3(n-10)^2 + 1 \\  (n-10)^2 &\geq 0 \text{ for } n \in \mathbb{N} \\  3(n-10)^2 &\geq 0 \\  3(n-10)^2 + 1 &> 0  \end{aligned}  $ <p>All terms in the pattern are positive/<i>al die terme in die patroon is positief</i></p> <p><b>OR/OF</b></p> $  \begin{aligned}  T_n &= 3n^2 - 60n + 301 \\  &= 3(n-10)^2 + 1  \end{aligned}  $ <p>T is a minimum valued function with minimum value 1 Range of T: <math>y \geq 1</math> All terms in the pattern are positive.</p> <p><i>T is funksie met minimum waarde van 1 Waardeversameling van T; <math>y \geq 1</math> al die terme in die patroon is positief</i></p> <p><b>OR/OF</b></p> $  \begin{aligned}  p &= \frac{-b}{2a} \\  &= \frac{(-60)}{6} \\  &= 10  \end{aligned}  $ $  \begin{aligned}  q &= 3(10)^2 - 60(10) + 301 \\  &= 1  \end{aligned}  $ <p>T is a minimum valued function with minimum value 1 Range of T: <math>y \geq 1</math> All terms in the pattern are positive.</p> <p><i>T is funksie met minimum waarde van 1 Waardeversameling van T; <math>y \geq 1</math> al die terme in die patroon is positief</i></p>	$\checkmark \checkmark T_n = 3(n-10)^2 + 1$ $\checkmark \checkmark \text{argument}$ (4)
-----	--	--



**QUESTION/VRAAG 5**

5.1	$\begin{aligned}f(-3) &= \frac{-3}{-3+2} + 1 \\&= 4\end{aligned}$	✓ answer/antw. (1)
5.2	$\begin{aligned}4 &= 2^{-x} - 4 \\8 &= 2^{-x} \\2^3 &= 2^{-x} \\x &= -3\end{aligned}$	✓ $4 = 2^{-x} - 4$ ✓ answer /antw. (2)
5.3	$\begin{aligned}x &= -2 \\y &= 1\end{aligned}$	✓ $x = -2$ ✓ $y = 1$ (2)
5.4	$\begin{aligned}y &> -4 \\ \text{OR/OF} \\y &\in (-4 ; \infty)\end{aligned}$	✓ answer/antw. (1) ✓ answer/antw. (1)



5.5	<p><i>y</i>-intercept/afsnit:</p> $y = \frac{-3}{0+2} + 1$ $= \frac{-1}{2}$ <p><i>y</i>-intercept/afsnit is <math>\left( 0 ; -\frac{1}{2} \right)</math></p> <p><i>x</i>-intercept/afsnit:</p> $0 = \frac{-3}{x+2} + 1$ $-1 = \frac{-3}{x+2}$ $-x - 2 = -3$ $-x = -1$ $x = 1$ <p><i>x</i>-intercept/afsnit is <math>(1 ; 0)</math></p>	✓ subst/verv $x = 0$ ✓ $y = \frac{-1}{2}$ ✓ subst/verv $y = 0$ ✓ simplification/vereenv. ✓ $x = 1$ (5)
5.6	$y = -x + c$ $1 = -(-2) + c$ $-1 = c$ $y = -x - 1$ <p><b>OR/OF</b></p> $y - 1 = -(x - (-2))$ $y = -x - 2 + 1$ $y = -x - 1$	✓ subst/verv ✓ answer/antw. (2) ✓ subst/verv ✓ answer/antw. (2)

5.7		<p><i>f</i></p> <ul style="list-style-type: none"> <li>✓ asympt/asimpt</li> <li>✓ Shape / vorm</li> <li>✓ <math>x</math> and <math>y</math> intercepts / afsnitte</li> </ul> <p><i>g</i></p> <ul style="list-style-type: none"> <li>✓ asymptote/asimpt</li> <li>✓ <math>x</math>-intercept/afsnit <math>(-2 ; 0)</math></li> <li>✓ <math>y</math>-intercept/afsnit <math>(0 ; -3)</math></li> </ul> (6)
5.8	<p><math>x \leq -3</math> or <math>-2 &lt; x \leq -1</math></p> <p><b>OR/OF</b></p> $x \in (-\infty ; -3) \cup (-2 ; -1]$	<ul style="list-style-type: none"> <li>✓ <math>x \leq -3</math></li> <li>✓ <math>-2 &lt; x \leq -1</math></li> </ul> (2) <ul style="list-style-type: none"> <li>✓ <math>(-\infty ; -3)</math></li> <li>✓ <math>(-2 ; -1]</math></li> </ul> (2)

4 WkW

## QUESTION/VRAAG 6

6.1	$0 = -x^2 - x + 6$ $x^2 + x - 6 = 0$ $(x+3)(x-2) = 0$ $x = -3 \text{ or } of \quad x = 2$ $B(-3; 0) \text{ and } C(2; 0)$	✓ $y = 0$ ✓ standard form/vorm ✓ factors/faktore ✓ both answers/beide antw (4)
6.2	$x = \frac{-b}{2a}$ $x = \frac{-( -1)}{2(-1)}$ $= -\frac{1}{2}$ <p><b>OR/ OF</b></p> $x = \frac{x_1 + x_2}{2}$ $= \frac{(-3) + (2)}{2}$ $= -\frac{1}{2}$	<b>NOTE/ LET WEL:</b> If answer only: award 2/2 marks Slegs antwoord: gee 2/2 punte
		✓ method/metode ✓ answer/antw. (2)
6.3	$f\left(-\frac{1}{2}\right)$ $= -\left(-\frac{1}{2}\right)^2 - \left(-\frac{1}{2}\right) + 6$ $= 6\frac{1}{4}$ TP / DP $\left(-\frac{1}{2}; 6\frac{1}{4}\right)$ Range/waardeversameling $y \in \left(-\infty; 6\frac{1}{4}\right]$ OR/OF $y \leq 6\frac{1}{4}$	✓ Subst ✓ $6\frac{1}{4}$ ✓ Answer/antw. (3)
6.4	D(0 ; 6) $m_{AD} = \frac{6-4}{0-(-2)}$ $= 1$ Equation of/vergelyking van g: $g(x) = x + 6$	✓ coordinates/koördinate D ✓ gradient. ✓ answer/antw (3)

6.5	Average/Gemid.gradient = gradient of/van g $= 1$	✓ answer/antw. (1)
6.6	$f(x) = -\left(x + \frac{1}{2}\right)^2 + \frac{25}{4}$ $h(x) = \left(x + \frac{1}{2} - 3\right)^2 - \frac{25}{4}$ $h(x) = \left(x - \frac{5}{2}\right)^2 - \frac{25}{4}$ <b>OR/OF</b> $f(x) = -x^2 - x + 6$ $h(x) = (x - 3)^2 + (x - 3) - 6$ $h(x) = x^2 - 5x$ $h(x) = \left(x - \frac{5}{2}\right)^2 - \frac{25}{4}$	✓ in the form/ in die vorm $f(x) = -\left(x + \frac{1}{2}\right)^2 + \frac{25}{4}$ ✓ $\left(x - \frac{5}{2}\right)^2$ ✓ $-\frac{25}{4}$ <b>OR/OF</b> ✓ $h(x) = (x - 3)^2 + (x - 3) - 6$ ✓ $\left(x - \frac{5}{2}\right)^2$ ✓ $-\frac{25}{4}$ (3)
6.7	$-3 < x < 2$ <b>OR/OF</b> $x \in (-3 ; 2)$	✓✓ answer/antw. (2) ✓✓ answer/antw. (2)
6.8	$r = -2$ By symmetry/deur simmetrie $p = 1$ $p - r = 3$ <b>OR/OF</b> $-x^2 - x + 6 = 4$ $-x^2 - x + 2 = 0$ $x^2 + x - 2 = 0$ $(x + 2)(x - 1) = 0$ $x = -2 \text{ or of } x = 1$ $r = -2$ $p = 1$ $p - r = 3$	✓ $r = -2$ ✓✓ $p = 1$ ✓ answer/antw. ✓ $r = -2$ ✓✓ $p = 1$ ✓ answer/antw. (4)

(4)  
[22]

**QUESTION/VRAAG 7**

7.1	$A = P(1 - i)^n$ $20000 = 80000(1 - i)^5$ $0,25 = (1 - i)^5$ $\sqrt[5]{0,25} = 1 - i$ $i = 1 - \sqrt[5]{0,25}$ $i = 0,24214417$ $i = 24,21\%$	✓ substitution into correct formula/ verv. in korrekte vorm ✓ simplification/ vereenv. ✓ answer/ antw. <span style="float: right;">(3)</span>
7.2	$1 + i_{eff} = \left(1 + \frac{i_{nom}}{m}\right)^m$ $1 + i_{eff} = \left(1 + \frac{0,05}{4}\right)^4$ $i_{eff} = 0,050945336\dots$ <p>Effective rate = 5,09 % p.a.</p>	✓ vorm/vorm ✓ subst/verv ✓ answer/antw. <span style="float: right;">(3)</span>
7.3	$A = P(1 + i)^n$ $= 30000 \left(1 + \frac{0,12}{12}\right)^{2 \times 12} \left(1 + \frac{0,108}{2}\right)^{4 \times 2}$ $= R 58 017,51$ <p><b>OR/ OF</b></p> $A = P(1 + i)^n$ $= 30000 \left(1 + \frac{0,12}{12}\right)^{2 \times 12}$ $= R38092,04$ $A = 38092,04 \left(1 + \frac{0,108}{2}\right)^{4 \times 2}$ $= R 58 017,51$	✓ $30000 \left(1 + \frac{0,12}{12}\right)^{2 \times 12}$ ✓ $\left(1 + \frac{0,12}{12}\right)^{2 \times 12}$ ✓ $\left(1 + \frac{0,108}{2}\right)^{4 \times 2}$ ✓ answer/antw. <span style="float: right;">(4)</span> ✓ $30000 \left(1 + \frac{0,12}{12}\right)^{2 \times 12}$ ✓ R38092,04 ✓ $38092,04 \left(1 + \frac{0,108}{2}\right)^{4 \times 2}$ ✓ answer/antw. <span style="float: right;">(4)</span>



<p>7.4</p> $  \begin{aligned}  A &= 25000\left(1+\frac{0,18}{12}\right)^{5 \times 12} - 8000\left(1+\frac{0,18}{12}\right)^{3 \times 12} + 4000\left(1+\frac{0,18}{12}\right)^{1,5 \times 12} \\  &= 25000\left(1+\frac{0,18}{12}\right)^{60} - 8000\left(1+\frac{0,18}{12}\right)^{36} + 4000\left(1+\frac{0,18}{12}\right)^{18} \\  &= \text{R } 52636,74  \end{aligned}  $ <p><b>OR/OF</b></p> $  \begin{aligned}  A_1 &= 25000\left(1+\frac{0,18}{12}\right)^{2 \times 12} \\  &= \text{R } 35\,737,57  \end{aligned}  $ <p>Amount in the account after the withdrawal:/<i>Bedrag in rekening na onttrekking</i>  <math>\text{R } 35\,737,5703 - \text{R } 8000</math>  <math>= \text{R } 27737,5703</math></p> <p>Amount in the account just before the deposit/<i>bedrag in rekening voor die deposito</i></p> $  \begin{aligned}  A_2 &= \text{R } 27737,5703\left(1+\frac{0,18}{12}\right)^{1,5 \times 12} \\  &= \text{R } 36262,45279  \end{aligned}  $ <p>Amount in the account just after the deposit/<i>Bedrag in rekening na onttrekking</i>  <math>\text{R } 36262,45279 + \text{R } 4000</math>  <math>= \text{R } 40262,45279</math></p> <p>Amount in the account at the end of 5 years/<i>Bedrag in rekening aan die einde van 5 jaar</i></p> $  \begin{aligned}  &= 40262,45279\left(1+\frac{0,18}{12}\right)^{1,5 \times 12} \\  &= \text{R } 52636,74  \end{aligned}  $	<p>✓ <math>\frac{0,18}{12}</math></p> <p>✓ <math>25000\left(1+\frac{0,18}{12}\right)^{5 \times 12}</math></p> <p>✓ <math>- 8000\left(1+\frac{0,18}{12}\right)^{3 \times 12}</math></p> <p>✓ <math>+ 4000\left(1+\frac{0,18}{12}\right)^{1,5 \times 12}</math></p> <p>✓✓ answer/antw.</p> <p>✓ <math>\frac{0,18}{12}</math></p> <p>✓ <math>25000\left(1+\frac{0,18}{12}\right)^{2 \times 12}</math></p> <p>✓ 27737,57</p> <p>✓ <math>27737,5703\left(1+\frac{0,18}{12}\right)^{1,5 \times 12}</math></p> <p>✓ 40262,45</p> <p>✓ answer/antw.</p>
--	---

**QUESTION/VRAAG 8**

8.1.1	<p style="text-align: right;">(B ; B) (B ; R) (R ; B) (R ; R)</p>	<ul style="list-style-type: none"> <li>✓ branches/takke</li> <li>✓ probabilities/waarskynlikhede</li> <li>✓ outcomes/uitkomste</li> </ul> <p style="text-align: right;">(3)</p>
8.1.2	$\begin{aligned} P(R, B) &= \frac{2}{5} \times \frac{3}{4} \\ &= \frac{3}{10} = 0,3 \end{aligned}$ <div style="border: 1px solid black; padding: 5px; margin-left: 20px;"> <b>NOTE/ LET WEL:</b>            If answer only: award 2/2 marks  <i>Slegs antwoord: gee 2/2 punte</i> </div>	<ul style="list-style-type: none"> <li>✓ <math>\frac{2}{5} \times \frac{3}{4}</math></li> <li>✓ answer/antwoord</li> </ul> <p style="text-align: right;">(2)</p>
8.2.1	$P(A) = 0,4$ $P(B) = 0,3$ $P(A \text{ or } B) = 0,58$ $\begin{aligned} P(A \text{ or } B) &= P(A) + P(B) - P(A \text{ and } B) \\ 0,58 &= 0,4 + 0,3 - P(A \text{ and } B) \\ P(A \text{ and } B) &= 0,12 \neq 0 \end{aligned}$ Events A and B are not mutually exclusive/ <i>Gebeurtenis A en B is nie onderlinguitsluitend nie</i>	<ul style="list-style-type: none"> <li><math>0,58 = 0,4 + 0,3 - P(A \text{ and } B)</math></li> <li><math>P(A \text{ and } B) = 0,12 \neq 0</math></li> <li>Not mutually exclusive/<i>nie onderling uitsluitend nie</i></li> </ul> <p style="text-align: right;">(3)</p>
8.2.2	$P(A \text{ and } B) = 0,12$ $\begin{aligned} P(A) \times P(B) &= 0,4 \times 0,3 \\ &= 0,12 \end{aligned}$ $\therefore P(A \text{ and } B) = P(A) \times P(B)$ A and B are independent events/ <i>is onafhanklik</i>	<ul style="list-style-type: none"> <li><math>P(A) \times P(B) = 0,4 \times 0,3</math></li> <li><math>P(A \text{ and } B) = P(A) \times P(B)</math></li> <li>A and B are independent/<i>is onafhanklik</i></li> </ul> <p style="text-align: right;">(3) [11]</p>

**QUESTION/VRAAG 9**

9.1	<p><math>n(S) = 80</math></p>	<ul style="list-style-type: none"> <li>✓ 14 or/of 12 or/of 15</li> <li>✓ <math>26 - x</math></li> <li>✓ <math>13 - x</math></li> <li>✓ 5</li> <li>✓ 3</li> </ul> <p>(5)</p>
9.2	$26 - x + 14 + x + 12 + 5 + 15 + 13 - x + 3 = 80$ $88 - 80 = x$ $x = 8$	<ul style="list-style-type: none"> <li>✓</li> <li><math>26 - x + 14 + x + 12 + 5 + 15 + 13 - x + 3</math></li> <li>✓ equating to/gelyk aan 80</li> </ul> <p>(2)</p>
9.3	<p>Number who chose Rugby only/aantal wat net rugby kies  <math>= 26 - 8</math>  <math>= 18</math></p>	<ul style="list-style-type: none"> <li>✓ answer/antw.</li> </ul> <p>(1)</p>
9.4	<p><math>P(\text{At least 2 types of sports}/\text{ten minste 2 sportsoorte})</math></p> $= \frac{12+14+15+8}{80}$ $= \frac{49}{80}$ <div style="border: 1px solid black; padding: 5px; margin-left: 20px;"> <b>NOTE/LET WEL:</b>            If answer only: award 3/3 marks  <i>Slegs antwoord : gee 3/3 punte</i> </div>	<ul style="list-style-type: none"> <li>✓ numerator/Noemer</li> <li>✓ denominator/Teller</li> <li>✓ answer/antw.</li> </ul> <p>(3)</p>
	<p><b>OR/OF</b></p> <p><math>P(\text{at least 2 types of sport}/\text{ten minste 2 sportsoorte})</math></p> $= 1 - \frac{18 + 5 + 5 + 3}{80}$ $= 1 - \frac{31}{80}$ $= \frac{49}{80}$	<ul style="list-style-type: none"> <li>✓ <math>\frac{18 + 5 + 5 + 3}{80}</math></li> <li>✓ method/metode</li> <li>✓ answer/antw.</li> </ul> <p>(3) [11]</p>

**TOTAL/TOTAAL: 150**